### Computable General Equilibrium (CGE) Modelling and SG's CGE model

This note provides a short introduction to CGE modelling and the key features of the Scottish Government's in-house CGE model.

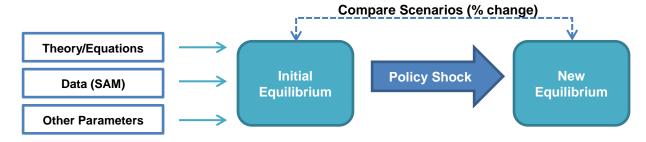
#### 1. What are CGE models?

- CGE models are large numerical models which combine economic theory with real economic data in order to derive computationally the impacts of policies or shocks in the economy.
- CGE models fit economic data to a set of equations which aim to capture the structure of
  the economy and behavioural response of agents (firms, households, government). This
  provides a framework to simulate policy changes and trace the impact on key economic
  variables, including income and expenditure flows.

## 2. How does CGE modelling work?

- The economic impact of the policy or economic shock being modelled is estimated by comparing the economy before and after the shock, as illustrated in the diagram below.
- The pre-policy baseline is generated by fitting the model equations and the behavioural parameters to the base year data. In general, this will mean that the base year to which the shock is applied will reflect the current structure of the economy. Our current model, for example, is calibrated using a wide range of sources of economic statistics for Scotland and the UK.
- The baseline assumes that the economy starts from a stable or equilibrium position i.e.
  markets clear, although some models, including the Scottish Government's own, relax
  some of these assumptions, for example by allowing for unemployment (see point 6
  below).
- When a policy change or economic shock is introduced, the economy converges to a new equilibrium, governed by the economic relationships as specified in the system of equations.
- The model derives a solution by finding a new set of prices and allocation of goods and factors such that the economy is in an equilibrium again.
- Some CGE models, such as the one used by the Scottish Government, are able to trace
  the path of adjustment to the new steady-state, whereas static ones will show long-run
  changes only. Modelling the adjustment path provides a much richer understanding of
  the evolution of the economy in response to a given shock or policy.

## Schema of CGE Modelling



# 3. Why are CGE models used?

 CGE models take into account the inter-dependencies between different sectors, agents and markets in the economy. CGE analysis can therefore shed light on the wider economic impact of policies and sometimes reveal their indirect or unintended effects.



- Since CGE models are grounded in economic theory, results can be explained using economic intuition, with the advantage that the economic impact can also be quantified using real data.
- CGE models capture both the economy's supply and demand side and therefore allow for an adjustment in both quantities and prices following a policy shock.
- Their main strength lies in their flexibility, as they can be adapted to simulate a wide range of policies and shocks.
- CGE models are widely employed by governments, international and research organisations, academics and private sector consultancies. The World Bank, OECD, IMF, HMRC, PWC have all made use of CGE frameworks in the past.

### 4. How does CGE differ from other modelling approaches?

- In contrast to *partial equilibrium* models, which focus on one section of the economy only, CGE models capture the entire economy and take into account the interactions and knock-on effects between its different segments.
- Unlike input-output models, which capture only the demand side and assume there are no capacity constraints, CGE models incorporate the supply side and hence allow for price movements.
- Compared to *macro-econometric forecasting* models, CGE models have a stronger foundation in economic theory. *Macro-econometric forecasting* models tend to be more data-driven, combining time series data with economic theory and often omit the detailed industrial data provided in CGE models.
- Whilst sharing many features with CGE models, Dynamic Stochastic General Equilibrium models (DSGE) aim to capture business cycle fluctuations and thus have a stronger focus on the shorter-term impacts. Unlike many CGE models, these types of models are less disaggregated and allow for random variation to account for uncertainty.

#### 5. Which data feed into the CGE model?

- The dataset which forms the backbone of the CGE model is the Social Accounting Matrix (SAM). It captures the flows of all economic transactions which take place in the economy in a single year. Its primary data sources are the Input-Output tables and the National Accounts, complemented by a range of other data on taxes, income and expenditure. This ensures that the model closely reflects the actual structure of the Scottish economy.
- Some parameter values, e.g. elasticities which govern the demand and supply responsiveness to price, are not determined within the model. Their values are mostly taken from empirical studies.
- However, most of the coefficients and exogenous variables have to be estimated using the base year data. This is done via a process called calibration which fits the data values to the model equations. If the model is calibrated correctly, it should replicate the base year equilibrium in the absence of any shocks.

## 6. What are the key features of the Scottish Government's CGE model?

- The Scottish Government's CGE model is a detailed one-region model of the Scottish economy which covers the onshore economic activity at a detailed industrial level.
- The model is based on a SAM for Scotland, that was constructed specifically for this purpose, and is complemented with data from other sources.
- The model was originally built by the University of Strathclyde, although the Scottish Government version has now undergone a number of in-house enhancements.



- The modelling framework is large-scale and contains around 200 groups of variables. Most of these groups of variables are further specified as variables for individual sectors.
- CGE models attempt to replicate the base structure of the economy. Although the base year is an equilibrium, this will capture features of real economy such as level of unemployment, spare capacity and export demand. For example, in the Scottish Government model, it is not assumed that the economy is operating at its full capacity in the base year and unemployment can go up or down depending on policy, as labour demand will depend on firms' optimising behaviour. Hence, not all markets will necessarily clear. This provides a degree of flexibility in the modelling.
- The model allows the impacts of policies and shocks to be traced through time. A steady-state should always be reached in the long-run when the model is correctly specified.
- The model's equations are specified and solved using GAMS (General Algebraic Modelling System) software - a high-level modelling system for mathematical programming and optimisation. Some modellers use a sub-system of GAMS - MSPGE (Mathematical Programming System for General Equilibrium) - that simplifies the modelling process for a specific type of CGE model.

## 7. What flexibility does the model offer?

- The framework provides flexibility to change a number of assumptions. This is useful for conducting scenario and sensitivity analyses.
- For example, the model offers a range of options with regards to specifying wage-setting behaviour and migration. It also allows for different assumptions to be made about the nature of households' and firms' future expectations.
- The underlying SAM data allows disaggregation into 104 industries. For computational
  and practical reasons these are usually aggregated into 25-35 broader sectors.
  However, the aggregation is flexible and can be adapted to policy for example, if the
  manufacturing sector is of greater interest for a particular simulation, more industrial
  detail can be included for that sector.
- The model can also be modified on a case-by-case basis to accommodate a range of various assumptions particular to specific policies. For example, various fiscal arrangements by which government spending in Scotland is determined can be specified.

## 8. Which policies can be modelled using the Scottish Government's CGE model?

- As with most CGE models, the Scottish Government's model is used most extensively
  for modelling fiscal policy scenarios. For example, the model is capable of simulating
  changes in various taxes, such as the Income Tax, Corporation Tax, Value Added Tax
  and National Insurance Contributions among others. It can also assess the impacts of
  changes in the level and profile of government spending.
- In addition, it can model the impacts of economic shocks such as changes in export demand, investment, productivity and labour supply. These shocks can be made specific for certain industries if desired.
- More detailed policies can also be modelled if sufficient additional data exists to modify the framework or do off-model analysis before running simulations.
- CGE models are versatile and can be amended and improved on a continuous basis to incorporate more detail about the economy. Hence, whilst it is possible to put together a list of policies and shocks that can be simulated, it would not be comprehensive.



#### 9. What is the role of the Rest of the UK in the model?

- Currently, the Rest of the UK (RUK) is treated as an exogenous region. Although trade
  and transfers to and from RUK are separated from the rest of the World, changes in
  policy in RUK cannot be modelled directly, although off-model analysis can still be
  incorporated into the modelling framework. At the moment, it is not possible to simulate
  how changes in policy in Scotland affect RUK endogenously in the model.
- The Scottish Government has commissioned an extension to the model that will extend
  the current framework into a 2-region model of the UK. It is currently in the process of
  testing and making final amendment to the model, whilst developing the internal capacity
  to use it for policy simulations.
- Once finalised, the new model will be capable of simulating policies in both Scotland and the rest of the UK separately and capture the interactions between the two economies. It is expected that the model will be operational in 2016.

## 10. Is the model capable of distributional analysis?

- Currently, the model does not differentiate between different types of households and hence is not capable of distributional analysis.
- However, the Scottish Government is currently co-funding research to develop an
  additional dataset incorporating household heterogeneity by income and type. The
  extension will allow distributional analysis to be taken forward which will increase the
  scope for modelling more detailed fiscal policy. This capacity is expected to be
  developed in 2016.

## 11. How long does it take to complete simulations?

- The length of time it takes to run a set of simulations depends on the policy or shock being modelled and each new simulation is likely to require an individual approach.
- Most simulations involve several stages, such as formulating the modelling strategy, making modifications to the programming code, interpreting simulations and performing sensitivity analyses.
- These are time-consuming tasks and undertaking new CGE simulations can take several
  weeks to complete, although this depends on the analysis in question. Updating previous
  work usually takes less resource, although analysts will still spend a significant amount
  of time on quality control.

The Office of the Chief Economic Adviser Scottish Government, December 2015



### **Useful external links**

#### University of Strathclyde

http://strathprints.strath.ac.uk/18035/

https://pure.strath.ac.uk/portal/en/publications/forward-looking-versus-myopic-regional-computable-general-equilibrium-models(9f91b193-31e1-4ff3-8752-d6d45fab9e9f)/export.html

#### **HMRC**

https://www.gov.uk/government/uploads/system/uploads/attachment\_data/file/263652/CGE\_model\_doc\_131204\_new.pdf

https://www.gov.uk/government/uploads/system/uploads/attachment\_data/file/301135/2014\_Regional\_CGE\_Research\_Report.pdf

## **GTAP**

https://www.gtap.agecon.purdue.edu/

#### World Bank

http://econ.worldbank.org/WBSITE/EXTERNAL/EXTDEC/EXTDECPROSPECTS/0,,content MDK:20279477~menuPK:538204~pagePK:64165401~piPK:64165026~theSitePK:476883,0 0.html

#### **IFPRI**

http://www.ifpri.org/sites/default/files/publications/mc5.pdf

## Textbook of Computable General Equilibrium Modelling

http://www.palgrave.com/page/detail/Textbook-of-Computable-General-Equilibrium-Modeling/?K=9780230248144

# Handbook of Computable General Equilibrium Modelling

http://store.elsevier.com/Handbook-of-Computable-General-Equilibrium-Modeling/isbn-9780444536358/

#### <u>EcoMod</u>

http://ecomod.net/

